#### WGS & SVs

Peter N. Robinson

Structural variants Array CGH SV Discover Poisson GC Content Read depth CNV Calling

## Genome Sequencing and Structural Variation

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Genomics: Lecture #10

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## Today

### WGS & SVs

### Peter N. Robinson

- Structural variants Array CGH
- Poisson
- GC Conten
- Read dept
- CNV Calling
- CNVnator

- Structural Variation
  - Deletions
  - Duplications
  - Inversions
  - Other
- Array CGH
- Algorithms for detecting structural variations from WGS data (Introduction)

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- Read-depth
- Split reads etc
- Read-depth Algorithm: Detailed Example

## Outline

### WGS & SVs

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## Structural variants

Array CGH

Structural

variants Array CGH SV Discove Poisson GC Conten Read depth

CNV Callin

Bioinformatics Approaches for Structural Variant Discovery

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Poisson

**5** GC Content

- 6 Read depth
- CNV Calling
- 8 CNVnator

## CNVs vs. SNVs

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# Single-nucleotide variants



## CNV



- Several thousand SNVs in typical exome (1% des Genoms)
- ca. 3–4 million SNVs in typical genome

- Hundreds/Thousands of CNVs per Genome
- average size 250,000 nt

(n.b.: avg. gene is ca. 60,000 nt)

## CNVs vs. SNVs

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CNV Calling

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## Single-Nucleotide Variants (SNV)

- Most missense, nonsense mutations, class also includes synonymous subsitutions and intergenic subsitutions
- Previously thought to be main source of interindividual genomic variability

Copy-Number Variants (CNV)

- Major class of genomic structural variation
- Alteration in normal number of copies of a genomic segment

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(Normal: 2 copies; Deletion: 1 copy; Duplication 3 copies.)

## **Structural Variation: Definition**

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Structural variants Array CGH SV Discovery Poisson GC Content Read depth CNV Calling

CNVnator

Structural variations (SV) are Genomic rearrangements that effect more than 1  $\rm Kb^1$ 

- Duplication and Amplification
- Deletion (often called Loss of heterozygosity if deletion occurs somatically, e.g., cancer)
- Translocation and Fusion
- Inversion
- Breakpoints at SV edges

<sup>1</sup>Yes, this definition is arbitrary!

## Inversion



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- A balanced structural variation (no loss/gain of genomic segment)
- Can be a neutral variation
- Can disrupt a coding sequence
- Can interrupt regulatory interactions

## Intrachromosomal translocation



• A balanced structural variation (no loss/gain of genomic segment)

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- Can be a neutral variation
- Can disrupt a coding sequence
- Can interrupt regulatory interactions

## Interchromosomal translocation



- A balanced structural variation (no loss/gain of genomic segment)
- Translocation between two different chromosomes
- Like other balanced SVs, can be neutral of disrupt coding sequences or regulatory interactions



• results in dosage abnormality of genes contained in deletion

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• Indirect regulatory imbalances also possible

## Duplication



- An **unbalanced** structural variation (gain of genomic segment)
- results in dosage abnormality of genes contained in deletion
- Indirect regulatory imbalances also possible

## Structural Variation: Distribution in Genome



### $\sim$ 1000 SVs >2.5kb per Person

Korbel JO et al (2007) Paired-end mapping reveals extensive structural variation in the human genome. Science 318:420–6.  $\langle \Box \rangle + \langle \Box \rangle + \langle$ 

## **Detection of Structural Variants**

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Structural variants

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	Techniques	Detection						Maximum resolution	Sensitivity
		Deletions and duplications	Insertions	Unbalanced translocations	Copy-neutral events				
					Balanced translocations	Inversions	LOH and UPD		
Early 1970s	Karyotyping/G-banding	Yes	Yes	Yes	Yes	Yes	No	Low (>several Mb)	Low
	FISH-based								
Early 1990s	CGH	Yes	No	Yes	No	No	No	Low (>several Mb)	High
Mid 1990s	M-FISH/SKY/COBRA	Yes	Yes	Yes	Yes	No	No	Low (>several Mb)	High
Late 1990s	RxFISH	Yes	Yes	Yes	Yes	Yes	No	Low (>several Mb)	High
	Array-based								
Early 2000s	1-Mb BAC array-CGH	Yes	No	Yes	No	No	No	Average (>1 Mb)	High
	Tiling-path BAC array-CGH	Yes	No	Yes	No	No	No	High (>50-100 kb)	High
	Oligonucleotide array-CGH	Yes	No	Yes	No	No	No	High (catalogue >1 kb, custom >400 bp)	Very high
Late 2000s	SNP arrays	Yes	No	Yes	No	No	Yes	High (>5-10 kb)	High
	NGS-based	Yes	Yes	Yes	Yes	Yes	Yes	Very high (hn level)	Very high

Abbreviations: BAC, bacterial articlai chromosome. CGH, comparative genomic hybridisation; COBRA, combined binary ratio labeling; FISH, fluorescence in situ hybridisation; COH, loss of heterotrayopsity. HTM: multiple: FISH Situation and the second secon

Still no method to reliably detect all SVsArray CGH currently the gold standard for CNVs

## Array-CGH



### A small heterozygous deletion in the $\beta$ -globin locus.

Urban AE et al. (2006) High-resolution mapping of DNA copy alterations in human chromosome 22 using high-density tiling oligonucleotide arrays. *Proc Natl Acad Sci U S A*. **103**:4534-9.

## **DNA Hybridization**



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Structura variants

### Array CGH

SV Discover Poisson

GC Conten

Read dept

CNV Calling

CNVnator



### DNA Hybridization:

- If two DNA strands are separated, they still "recognize" their opposite (reverse complementary) strand.
- denaturation: Heat DNA until strands separate
- renaturation (hybridization): cool slowly and allow reverse complementary to anneal to one another

## Array-CGH





Structura variants

Array CGH

Poisson

GC Conten

Read dept

CNV Calling

CNVnator



 Ratio of 2 fluorescent signals indications loss or gain of DNA segment

## Array-CGH

### WGS & SVs

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Structural variants

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SV Discovery

Poisson

GC Conte

Read dept

CNV Calling

CNVnator

Array CGH can detect

- Deletions
- Duplications (& and other gains in copy number)
- More complex copy number changes (e.g., mixed)



Urban AE et al. (2006) High-resolution mapping of DNA copy alterations in human chromosome 22 using

high-density tiling oligonucleotide arrays. Proc Natl Acad Sci U S A. 103:4534-9.

## Array-CGH: Indications in Human Genetics

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- Structural variants
- Array CGH
- SV Discovery
- Poisson
- GC Conten
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- Intellectual disability or developmental delay of unknown cause
- Congenital malformation or facial dysmorphism
- Autism or suspicion of a specific chromosomal disorder

Array-CGH is a screening investigation to investigate nearly the entire genome for CNVs in an un targeted fashion. Many findings are "new" and may be difficult to interpret: cause of a disease or neutral polymorphism?

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## Outline

### WGS & SVs

Peter N. Robinson

### Structural variants

Array CGH

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Array CGH

SV Discovery

Poisson GC Conter Read deptl CNV Callin

**CNV**nator

- 6 Read depth
- CNV Calling
- 8 CNVnator

## **Bioinformatics Approaches for Structural Variant** Discovery

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# Bioinformatics Approaches for SV Discovery with WGS data

### WGS & SVs

### Peter N. Robinson

Structural variants Array CGH

### SV Discovery

Poisson

- GC Content
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Several characteristics of NGS data can be exploited for identification of different kinds of structural variants

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- Read depth
- Read pairs
  - Orientation of mates
  - Ø Distance of aligned mates to one another
- Split reads
- Fine mapping of breakpoints by local assembly

## Paired NGS Reads

### WGS & SVs

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Structural variants Array CGH SV Discovery Poisson GC Content Read depth CNV Calling Paired sequences are extremely useful for read mapping in whole genome sequencing because we not only have the information about the DNA sequences but also the distance and orientation of the two mapped reads to one another. There are two major classes of paired sequences.

- Paired end. Fragment libraries<sup>2</sup> are sequenced from both ends. The sequencing direction is from the ends towards the middle.
- Mate-pair libraries. We will review this today

<sup>&</sup>lt;sup>2</sup>As discussed in the very first lecture.  $\langle \Box \rangle \langle \Box \rangle \langle \Xi \rangle \langle \Xi \rangle \langle \Xi \rangle \langle \Xi \rangle \langle \Box \rangle$ 

## Mate pair

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### Structural variants

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### SV Discovery

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## Construction of Illumina mate-pair sequencing libraries.

Fragments are end-repaired using biotinylated nucleotides

- After circularization, the two fragment ends (green and red) become located adjacent to each other
- The circularized DNA is fragmented, and biotinylated fragments are purified by affinity capture. Sequencing adapters (A1 and A2) are ligated to the ends of the captured fragments
- 4
  - the fragments are hybridized to a flow cell, in which they are bridge amplified. The first sequence read is obtained with adapter A2 bound to the flow cell
- (
- The complementary strand is synthesized and linearized with adapter A1 bound to the flow cell, and the second sequence read is obtained
- The two sequence reads (arrows) will be directed outwards from the original fragment.



Berglund EC et al. (2011). Investig Genet 2:23.

## Paired-end vs. Mate pair



If we have two 75 bp paired-end reads with a 100bp middle piece, the insert size is calculated as  $2 \times 75 + 100 = 250$  nt. The fragment size is insert size plus length of both adapters ( $\approx 120$  nt extra).

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## **Read depth** WGS & SVs Peter N Analysis of read depth can identify deletion/duplications Robinson Array CGH SV Discovery Heterozygous Deletion? Mappability Issue? Poor "sequencability"?

## **Read depth**



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## Characteristic signatures of paired-end sequences



graphic credit: Victor Guryev

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## **Deletions in WGS Data**



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## **Deletions in WGS Data**



## Insertions in WGS Data



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## Insertions in WGS Data

### WGS & SVs

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Structural variants Array CGH SV Discovery Poisson GC Content Read depth  
SV classes
Read pair
Read depth
Split read
Assembly

Novel sequence insertion
Image: Control of the security of the securety of the security of the securety of the security of

Read pairdecreased interpair mapping distanceRead depthnot applicable3Split readsingle read is split into two segments<br/>surrounding novel insertion sequenceAssemblyassembled sequence with inserted<br/>novel sequence

 $<sup>^{3}</sup>$ Novel sequence will not map to genome

## Inversions in WGS Data



CNVnator

What are the signals that let us detect a inversion?

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## Inversions in WGS Data

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Read pair	aberrant mapping (>> instead of
	>< ) and interpair distance
Read depth	not applicable <sup>4</sup>
Split read	single read is split into two segments
	one of which is inverted
Assembly	assembled sequence with inverted se-
	quence

## **Duplications in WGS Data**



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## **Duplications in WGS Data**

### WGS & SVs

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- GC Conten
- Read dept
- CNV Callin
- **CNV**nator



Read pair	aberrant mapping (<> instead of
	>< ) and interpair distance
Read depth	increasd
Split read	single read is split into end of one du-
	plicated block followed by beginning
	of next block
Assembly	assembled sequence with duplicated
	sequence

Graphics credit: Le Scouarnec and Gribble SM Heredity (Edinb). 2012; 108:75-85.

## **Translocations in WGS Data**





• In sum: There are many different signals that are used for SV detecction. Different read types have distinct attributes

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## **Read depth**

### WGS & SVs

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GC Content Read depth CNV Calling CNVnator In the remainder of this lecture, we will examine how read depth analysis can be used to search for CNVs. We will concentrate on three topics.

- Poisson distribution: Review
- G/C dependence
- Simplified version of algorithm in Yoon et al.<sup>5</sup>

<sup>&</sup>lt;sup>5</sup>Sensitive and accurate detection of copy number variants using read depth of coverage. *Genome Res.* 2009;**19**:1586–92.
### Poisson

#### WGS & SVs

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Structural variants Array CGH SV Discovery

Poisson

GC Content Read depth CNV Calling CNVnator A Poisson experiment is a statistical experiment that has the following properties:

- The experiment results in outcomes that can be classified as successes or failures.
- The average number of successes (µ) that occurs in a specified region is known.
- The probability that a success will occur is proportional to the size of the region.
- The probability that a success will occur in an extremely small region is virtually zero.

The "region" can be a length, an area, a volume, a period of time, etc.

Early use of Poisson distribution: Ladislaus Bortkiewicz (1898): investigation of the number of soldiers in the Prussian army killed accidentally by horse kick.



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### Poisson

#### WGS & SVs

Peter N. Robinson

Structural variants Array CGH SV Discover Poisson GC Content Read depth CNV Calling  $P(X=k) = \frac{\lambda^k e^{-\lambda}}{k!} \tag{1}$ 

- *k* = number of occurrences
- $\lambda = average occurrences/time interval$

For example, if the average number of soldiers killed by being kicked by a horse each year in each of 14 cavalry corps is 1.7, what is the probability of 4 soldiers being killed in one year?

$$P(X=4) = \frac{(1.7)^4 e^{-(1.7)}}{4!} = 0.063$$
(2)

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In R,

> dpois(4,1.7) [1] 0.06357463

### Poisson



For X ~ Poisson(λ), both the mean and the variance are equal to λ

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### Poisson and Read counts

#### WGS & SVs

Peter N Robinson

Array CGH

#### Poisson

Many NGS algorithms model read counts as a Poisson distribution

- Segment the genome into Windows (e.g., 1000 bp).
- Count number of reads in each Window
- All else equal, we expect half as many reads as normal in the case of a deletion, and 1.5 times as many reads as normal in the case of a duplication

$$\lambda = \frac{NW}{G} \quad w$$

 $\frac{1}{2}$  /here  $\begin{cases} N & \text{Total number of reads} \\ W & \text{size of window} \\ G & \text{Size of genome} \end{cases}$ (3)

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- CNVnator

The Poisson distribution can be derived as a limiting form of the binomial distribution in which n is increased without limit as the product  $\lambda = np$  is kept constant.

- This corresponds to conducting a very large number of Bernoulli trials with the probability *p* of success on any one trial being very small.
- This suggests we can approximate the Poisson distribution by the Normal distribution

The central limit theorem: the mean of a sufficiently large number of independent random variables, each with finite mean and variance, is approximately normally distributed

#### WGS & SVs

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Structural variants Array CGH SV Discovery

#### Poisson

GC Content Read depth CNV Calling CNVnator For sufficiently large values of  $\lambda$ , (say  $\lambda > 1,000$ ), the Normal( $\mu = \lambda, \sigma = \sqrt{\lambda}$ ) Distribution is an excellent approximation to the Poisson( $\lambda$ ) Distribution.

If  $\lambda$  is greater than about 10, then the Normal Distribution is a good approximation if an appropriate continuity correction is performed.

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#### WGS & SVs

#### Peter N. Robinson

Structural variants Array CGH SV Discovery Poisson

```
GC Content
Read depth
CNV Calling
CNVnator
```

 Finally, we can check in R that the Normal is a reasonable approximation to the Poisson (it is not an extremely close approximation for λ in this range yet)<sup>6</sup>.

```
> pnorm(25,mean=20,sd=sqrt(20),lower.tail=FALSE)
[1] 0.1317762
> ppois(25,20,lower.tail=FALSE)
[1] 0.112185
```

For this reason, we will see the Normal distribution (often a z-score) used to calculate read depth statistics.

<sup>6</sup>It would be better for  $\lambda = 50$  and better yet for  $\lambda = 1000$  or above. So  $\sim$ 



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grapic: wikipedia

### **GC** Content



grapic: wikipedia

• The GC content  $\frac{G+C}{A+C+G+T}$  of a sequence affects many properties, e.g., annealing temperature of PCR primers

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### **GC** Content in Bioinformatics

#### WGS & SVs

Peter N. Robinson

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Read depth CNV Callin

CNVnator

GC content is correlated with multiple other parameters, and bioinformatics analysis often needs to take this into account

- $\uparrow$  GC content  $\Leftrightarrow$   $\uparrow$  mRNA stability
- Giemsa dark bands (cytogenetics) ⇔ locally GC-poor regions compared with light bands
- Housekeeping (ubiquitously expressed) genes in the mammal genome ⇔ on average slightly GC-richer than tissue-specific genes.
- Silent-site GC content correlates with gene expression efficiency in mammalian cells.

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for instance...

### **GC** Content in Genomics

#### WGS & SVs

#### Peter N. Robinson

- Structural variants Array CGH SV Discover Poisson GC Content
- Read depth CNV Calling
- CNVnator

GC content is can confound the results of a number of genomics experiments

- Dependence between fragment count (read coverage) and GC content found in Illumina sequencing data.
- The GC effect is unimodal: both GC-rich fragments and AT-rich fragments  $\Leftrightarrow$  underrepresented.
- RNA-seq: GC-rich and GC-poor fragments tend to be under-represented in RNA-Seq, so that, within a lane, read counts are not directly comparable between genes
- ChIP-seq: Peaks (profiles) correlate positively with genomic GC content
- Whole genome sequencing: GC content may correlate positively with read depth

See for instance: Benjamini Y, Speed TP (2012) Summarizing and correcting the GC content bias in high-throughput sequencing. Nucleic Acids Res 40:e72.

### **Read Depth**

#### WGS & SVs

Peter N. Robinson

Structural variants Array CGH SV Discovery Poisson GC Content Read depth CNV Calling We can get a simple picture of the distribution of reads acrosss a chromosome by counting how many reads start in a given chromosomal window.

### Basic workflow

- Align reads from high or low coverage genome sequencing
- Count the number of reads that begin in each window of size  $N^7$
- Plot (eyeball-o-metrics)

There is a tutorial on how to do the next few analysis steps on the website.

<sup>7</sup>The best size for *N* will depend on the questions, the coverage, and the algorithm, but might be between 1000-100,000.

### **Read Depth**

### WGS & SVs

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## This is a typical plot showing the raw read depth following genome sequencing.

Thousand genomes project, individual HG00155, chromosome 11, low-coverage



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### GC content vs. Read Depth

### WGS & SVs Peter N. Robinson loess-smoothed regression line is shown

Array CGH

Read depth





#### WGS & SVs

#### Peter N. Robinson

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CNVnator

## With this information in hand, we will discuss a leading algorithm used to detect CNVs in genomic data, **CNVnator**.

Abyzov A, Urban AE, Snyder M, Gerstein M (2011) CNVnator: an approach to discover, genotype, and characterize typical and atypical CNVs from family and population genome sequencing. *Genome Res* **21**:974-84.

• CNVnator makes use of a number of nice ideas to provide good CNV calls

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- GC content correction
- Partitioning of bins with mean shift technique
- statistical hypothesis testing to call CNVs

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- CNV Calling
- CNVnator

- Average RD signal distribution in produced segments.
- 3 clear peaks
  - around the genomic RD average (no CNVs)
  - a half of that (heterozygous deletion)
  - one and one-half of that (duplication of one haplotype).
- The average genomic RD signal is ~ 77 reads.



#### WGS & SVs

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- CNVnator

- Let us examine panel B
- Distribution of the average RD signal difference for **neighboring segments**.
- One cluster of neighboring segments has similar average RD signals (peak around zero).
- The other cluster has an average signal difference of ~half of the genomic average RD signal.
- ... changes in average RD signal at two neighboring segment boundaries cluster, and these clusters can be explained by partitioning that includes deletions and duplications



### Partitioning genome into CN segments

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CNV Callin

**CNV**nator

- Distribution of the average RD signal difference at the left and right boundary for each segment.
- The clusters originate due to various combinations of segments with different RD signals.

Cluster 3: CNV neutral.

Cluster 2: Deletion begins on left side

Cluster 4: Insertion begins on left side

etc.



# **CNV**nator: Dealing with multiply mappable reads



#### Peter N. Robinson

Structural variants Array CGH SV Discovery Poisson GC Content Read depth

**CNV**nator



Treangen TJ and Steven L. Salzberg SL (2012) Nature Reviews Genetics 13:36-46

- three different tandem repeats with two copies each
- Left: read aligns equally well to both X<sub>1</sub> and X<sub>2</sub>
- Middle: read aligns slightly better to Y<sub>1</sub> than to Y<sub>2</sub>
- Right: read aligns perfectly to Z<sub>1</sub>, whereas its alignment to Z<sub>2</sub> contains three mismatches

When a read (pair of reads) can map equally well to two or more locations, then one is randomly chosen. In such cases, the associated mapping quality is zero.

## **CNV**nator: Dealing with multiply mappable reads

#### WGS & SVs

#### Peter N. Robinson

- Structural variants Array CGH SV Discovery Poisson GC Content Read depth
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- CNVnator

• Calling a CNV in particular regions is confounded by the presence of the same (or very similar) copies of that region in the reference genome.

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 The RD signal for a CNV in these regions is effectively smeared (due to random placement of nonuniquely mapped reads) over all copies

## Example: Dealing with multiply mappable reads

### WGS & SVs Peter N Robinson Reference ABB' C Arrav CGH Deletion AB C • Consider the situation where the reference has two nearly identical segmental duplications, B and B' The sequenced individual has a homozygous deletion of B' **CNV**nator Reads that originate from B in the sample will distribute equally between B and B' in the reference

- Thus, both B and B' have half of the average RD (i.e., copy number [CN] = 1)
- A naive analysis would identify both B and B' as heterozygous deletions

# **CNV**nator: Dealing with multiply mappable reads





Structural variants Array CGH SV Discover Poisson GC Content Read depth CNV Calling CNVnator



Distribution of fraction of q0 mapped reads in the regions of predicted CNVs

- Quality zero (q0) reads commonly occur in CNV regions
- The distribution of the fraction of q0 reads in the called CNV regions has peaks around 0 and 100%
- CNVnator considers a CNV region redundant if the fraction of q0 reads in the called CNV regions is > 50%.

### **GC** Adjustment



average RD signal over all bins, and  $\overline{RD}_{GC}$ : average RD signal over all bins with the same GC content as in the bin.

This correction effectively eliminates correlation of RD signal with GC content

### Partitioning

#### WGS & SVs

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**CNV**nator

The bin size used by CNVnator is typically 100-300 nucleotides, but many CNVs are much larger than this. We would therefore like to partition a chromosome into segments with the same copy number.

The general flow of the algorithm can be summarized as

- divide genome into bins, count reads
- Use partitioning algorithm to join adjancent bins together
- statistical postprocessing to call deletions/duplications



Xi R et al. (2011) Copy number variation detection in whole-genome sequencing data using the Bayesian information criterion. *PNAS* 108:E1128-36.

### Mean shift: Kernel density estimation

#### WGS & SVs

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- Given a random sample  $X_1, X_2, \ldots, X_n$  with a continuous univariate density f
- The kernel density estimator with kernel *K* and **bandwidth** *h* is

$$\hat{f}(x,h) = \frac{1}{nh} \sum_{i=1}^{n} K\left(\frac{x - X_i}{h}\right)$$
(5)

- Center of kernel is placed right over each data point.
- Influence of each data point is spread about its neighborhood.
- Contribution from each point is summed to overall estimate

### Mean shift: Kernel density estimation

WGS & SVs

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Structural variants Array CGH SV Discover Poisson GC Content Read depth CNV Calling CNVnator • Consider use of Gaussian kernel to estimate the density of the following data

$$\hat{f}(x,h) = \frac{1}{\sqrt{2\pi}\sigma} \sum_{i=1}^{n} e^{-\left(\frac{x-X_i}{2\sigma^2}\right)}$$
(6)



### Mean shift: Kernel density estimation

WGS & SVs

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• The bandwidth is a scaling factor that controls how wide the probability mass is spread around a point.

• it controls the smoothness or roughness of a density estimate



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### Mean shift: Read count bins

#### WGS & SVs

Peter N. Robinson

Structural variants Array CGH SV Discovery Poisson GC Content Read depth CNV Calling CNVnator In CNVnator, each read count bin is represented as a point in 2 dimensional space  $x_i = (i, r_i)$ , where  $r_i$  is the signal bin index using a two-dimensional Gaussian kernel

$$F(x_i) = norm \sum_{j \neq i}^{n} e^{-\left(\frac{j-i}{2H_b^2}\right)} e^{-\left(\frac{r_j - r_i}{2H_r^2}\right)}$$
(7)

j is the index of neighboring bins,  $H_b$  and  $H_r$  are the bandwidths for the bin index and RD signal accordingly, and *norm* is the normalization factor.

• The mean-shift vector is the gradient of this function  $\nabla F(x_i) = \begin{pmatrix} \frac{\partial F}{\partial i} \\ \frac{\partial F}{\partial r} \end{pmatrix}$ (8)

### Mean shift: Read count bins

#### WGS & SVs

Peter N. Robinson

Structural variants Array CGH SV Discovery Poisson GC Content Read depth CNV Calling CNVnator Since we are only interested in the direction of the gradient along the bins, we calculate

$$\frac{\partial F}{\partial i} = \frac{\partial}{\partial i} \operatorname{norm} \sum_{j \neq i}^{n} e^{-\left(\frac{j-i}{2H_{b}^{2}}\right)} e^{-\left(\frac{r_{j}-r_{i}}{2H_{r}^{2}}\right)}$$
$$= \operatorname{norm} \sum_{j \neq i}^{n} -(j-i) e^{-\left(\frac{j-i}{2H_{b}^{2}}\right)} e^{-\left(\frac{r_{j}-r_{i}}{2H_{r}^{2}}\right)}$$

We are now only interested in the direction of  $\frac{\partial F}{\partial i}$ , i.e., whether it is pointing to the right ( $\frac{\partial F}{\partial i} > 0$  or to the left ( $\frac{\partial F}{\partial i} < 0$ ). Thus we do not need to calculate *norm*, which is always positive.

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### Mean shift: Read count bins

#### WGS & SVs

#### Peter N. Robinson

Structural variants Array CGH SV Discovery Poisson GC Content Read depth CNV Calling

CNVnator

For each bin, i.e., data point, the mean-shift vector points in the direction of bins with the most similar RD signal. Segment breakpoints are determined where two neighboring vectors have opposite directions but do not point to each other.



#### WGS & SVs

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**CNV**nator

CNVnator uses some interesting heuristics to estimate the optimal bandwidth in order to come up with a final partitioning of bins, which we will not go into here. Finally, the analysis is performed with a one-sample t test

Recall: To test the null hypothesis that a population mean is equal to a specified value  $\mu_0$ , one uses the t statistic

$$t = \frac{\overline{x} - \mu_0}{s/\sqrt{n}} \tag{9}$$

where  $\overline{x}$  is the sample mean, s is the sample standard deviation of the sample and n is the sample size. The degrees of freedom used in this test are n1.

#### WGS & SVs

#### Peter N. Robinson

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**CNV**nator

### The t test for CNVnator is formulated as

$$t = \frac{\overline{RD}_{global} - \overline{RD}_{segment}}{s_{segment}/\sqrt{n}}$$
(10)

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where *n* is the number of bins within the segment,  $\overline{RD}_{segment}$  is its average RD signal, and  $s_{segment}$  is the signal standard deviation.



atypical CNVs from family and population genome sequencing. Genome Res 21:974-84.

### **CNV Calling via Read Depth**



Yoon et al. Sensitive and accurate detection of copy number variants using read depth of coverage. Genome Res. 2009;19:1586–92.  $\langle \Box \rangle \langle \Box \rangle \langle$
## Summary

## WGS & SVs

## Peter N. Robinson

- Structural variants Array CGH SV Discovery Poisson GC Content Read depth
- CNV Calling

CNVnator

## What you should take away from this lecture

- The various kinds of signals used to detect structural variants (SVs) in NGS data
- The various kinds of SVs and what effects they have on NGS reads
- Basic steps in using read depth to identify copy number variations (CNVs)

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• GC bias

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